

Semester Pattern: 2023-24

[January Session]

Instructions to submit **First Semester** Assignments

- 1. Following the introduction of semester pattern, it becomes **mandatory for** candidates to submit assignment for each course.
- 2. Assignment topics for each course will be displayed in the A.U, CDOE website (**www.audde.in**).
- Each assignment contains 5 questions and the candidate should answer all the 5 questions. Candidates should submit assignments for each course separately. (5 Questions x 5 Marks =25 marks).
- Answer for each assignment question should not exceed 4 pages. Use only A4 sheets and write on one side only. Write your Enrollment number on the top right corner of all the pages.
- 5. Add a template / content page and provide details regarding your Name, Enrollment number, Programme name, Code and Assignment topic. Assignments without template / content page will not be accepted.
- 6. Assignments should be handwritten only. Typed or printed or photocopied assignments will not be accepted.
- Send all First semester assignments in one envelope. Send your assignments by Registered Post to The Director, Center for Distance and Online Education, Annamalai University, Annamalai Nagar – 608002.
- 8. Write in bold letters, "**ASSIGNMENTS FIRST SEMESTER**" along with PROGRAMME NAME on the top of the envelope.
- 9. Assignments received after the **last date with late fee** will not be evaluated.

Date to Remember

Last date to submit First semester assignments: 15.04.2024Last date with late fee of Rs.300 (three hundred only): 30.04.2024

Dr. T. SRINIVASAN

Director

(S018) - M.Sc MATHEMATICS

AY-2023-24 – FIRST YEAR - I – SEMESTER

(JANUARY SESSION) - Assignment Questions

018E1110 - ABSTRACT ALGEBRA

- 1. a) Prove that any group of prime order is cyclic and can be generated by any element of the group except the identity.
 - b) If H and K are finite subgroups of a group G of order O(H) and O(K) respectively then prove that $O(HK) = \frac{O(H)O(K)}{O(H \cap K)}$.
- 2. a) State and Prove cauchy's theorem for abelian groups.
 - b) State and Prove sylow's theorem for abelian groups.
 - c) Let $\varphi: G \to \overline{G}$ be a homomorphism with ker *K* and \overline{N} be a normal subgroup of \overline{G} , where $N = \{x \in G : \varphi(x) \in \overline{N}\}$ then prove that $\frac{G}{N} \approx \frac{\overline{G}}{\overline{N}}$
- 3. a) Prove that every integral domain can be imbedded in a field.
 - b) Prove that the ideal A = (p(x)) in F[x] is a minimal ideal if and only if p(x) is irreducibleover F.
 - c) Let *V* is finite-dimensional and *W* is a subspace of *V* then prove that *W* is finite dimensional, dim $W \le \dim V$ and dim $V/W = \dim V - \dim W$
- 4. a) Prove that $I(G) \approx \frac{G}{Z}$, where I(G) is the group of inner

automorphisms of G and Z is the centre of G.

- b) Prove that an ideal M of an Euclidean ring R is a maximal ideal if and only if the ideal M is the principal ideal generated by a prime element of R.
- a) If F is any field, prove that the ring F(x)of all polynomials in x over F is a Euclidean ring.
 - b) If V and W are of dimensions m and n respectively over F then prove that Hom (V, W) is of dimension mn over F.

018E1120 - REAL ANALYSIS

- 1. a) State and Prove Intermediate value theorem for Derivatives.
 - b) State and Prove Chain rule for Derivatives.
- 2. a) Let f be of bounded variation on [a, b] and V be defined on [a, b]as follows $V(x) = V_f(a, x)$ if $a \le x \le b$ and V(a) = 0 then Prove that
 - Vis an increasing function on [a, b]. i.
 - ii. (V - f) is an increasing function on [a, b].
 - b) Write the Additive property of Total variation.
- 3. a) If $f \in R(\alpha)$ on [a, b], then prove that $\alpha \in R(f)$ on [a, b] and $\int_{a}^{b} f \, d\alpha + \int_{a}^{b} \alpha \, df = \alpha (b) f(b) - \alpha (a) f(a).$ b) State and Proveeuler's summation formula.
- 4. a) State and Prove First Mean Value theorem for Riemann Stieltges Integral.
 - b) Write the necessary conditions for existence of Riemann- Stieltges Integrals.
- 5. a) State and Prove Tauber's theorem.
 - b) State and Prove Abel's limit theorem.

018E1130 - DIFFERENTIAL EQUATIONS AND APPLICATIONS

- 1. a) Solve $y'' + 2y' + 2y = \frac{e^{-x}}{\cos^3 x}$ by using the method of variation of parameter.
 - b) Solve $y'' + 4y = 4 \tan 2x$ by using the method of variation of parameter.
- 2. a) Solve the Bessel equation $x^2y'' + xy' + (x^2 n^2)y = 0$ in series taking 2n as non- integral.
 - b) Solve the series the Legendre's equation $(1 x^2)y'' 2xy' + 4y = 0$ near the singular point x = 1.
- 3. a) Find the general solution of $(x^2 1)y'' + (5x + y)y' + (n + 1)ny = 0$.
 - b) Drive the Gauss's hyper geometric equation.
- 4. a) Prove that

$$\int_{-1}^{1} P_m(x) P_n(x) dx = \begin{cases} 0 & \text{if } m \neq n \\ \frac{2}{2n+1} & \text{if } m = n \end{cases}$$

b) Find the first three terms of the Legendre series $f(x) = e^x$.

5. a) Prove that

$$\int_{0}^{1} x J_{p}(\lambda_{m}x) J_{p}(\lambda_{n}x) dx = \begin{cases} 0 & \text{if } m \neq n \\ \frac{1}{2} J_{p+1}(\lambda_{n})^{2} & \text{if } m = n \end{cases}$$

b) Prove that

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$$J_p - J'_{-p} - J'_p J_{-p} = \frac{-2\sin p\pi}{\pi x}$$

018E1140 - ANALYTICAL MECHANICS

- a) Explain the kinetic energy of a rigid body with a fixed point and angular momentum of a rigid body.
 - b) Explain general motion of the spherical pendulum.
- 2. a) Explain the equation of motion of a particle relative to the Earth surface.
 - b) Explain general motion of a top.
- 3. a) Explain the Lagrange's equation for any simple dynamical system.
 - b) State and prove Hamilton's principle.
- 4. a) Explain the Angular Momentum and General Motion of a Rigid body.
 - b) Discuss the motion of a simple pendulum in terms of elliptic functions and the Periodic Time of the simple pendulum
- 5. a) Explain the motion of a Rolling disk.
 - b) Describe the Lagrange's equations for motion of a particle in a plane.